

# Strong Second-Harmonic Generation in Atomic Layered GaSe

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**Supporting Information** 

**ABSTRACT:** Nonlinear effects in two-dimensional (2D) atomic layered materials have recently attracted increasing interest. Phenomena such as nonlinear optical edge response, chiral electroluminescence, and valley and spin currents beyond linear orders have opened up a great opportunity to expand the functionalities and potential applications of 2D materials. Here we report the first observation of strong optical second-harmonic generation (SHG) in monolayer GaSe under nonresonant excitation and emission condition. Our experiments show that the nonresonant SHG intensity of GaSe is the strongest among all the 2D atomic crystals measured up to day. At the excitation wavelength of 1600 nm, the SHG signal from monolayer GaSe is around 1-2 orders of magnitude larger than that from monolayer MoS<sub>2</sub> under the same excitation power. Such a strong nonlinear signal facilitates the use of polarization-dependent SHG intensity and SHG mapping to investigate the symmetry properties of this material: the monolayer GaSe shows 3-fold lattice symmetry with an intrinsic correspondence to its geometric triangular shape in our growth condition; whereas the bilayer GaSe exhibits two dominant stacking orders: AA and AB stacking. The correlation between the stacking orders and the interlayer twist angles in GaSe bilayer indicates that different triangular GaSe atomic layers have the same dominant edge configuration. Our results provide a route toward exploring the structural information and the possibility to observe other nonlinear effects in GaSe atomic layers.

**S** ince the discovery of graphene<sup>1,2</sup> and the rise of  $MoS_{2,}^{3,4}$  two-dimensional (2D) atomic layered materials have come to the central stage of material study due to their distinct properties to the bulk form and potential applications in nanoscience and technology.<sup>5–10</sup> Recently, nonlinear effects in 2D atomic layered materials have attracted increasing interest. Salient examples include nonlinear optical responses from edge states in  $MoS_{2,}^{11}$  chiral light emission in WSe<sub>2</sub> induced by nonlinear carrier diffusion shift,<sup>12</sup> and nonlinear valley and spin currents in graphene, transition-metal dichalcogenides, or

GaSe.<sup>13</sup> The pursuit of strong nonlinear effects in 2D materials is therefore of great importance in expanding their functionalities and potential applications beyond linear effects.

Among the large family of 2D materials, atomic layered GaSe has been receiving intensive attention. Monolayer and few-layer GaSe has high responsibility in photocurrent generation;<sup>14-18</sup> the thinning of GaSe from bulk to few layers will drive a direct-to-indirect bandgap transition;<sup>18,19</sup> the hole doping can induce tunable magnetism in monolayer GaSe;<sup>20</sup> and appreciable nonlinear spin and valley currents can be generated by electrical bias or temperature gradient in monolayer GaSe.<sup>13</sup> Especially, as bulk GaSe is a well-known nonlinear crystal with secondorder optical nonlinear coefficient 2 orders of magnitude larger than that of the widely used LiNbO3 crystal,<sup>21,22</sup> one may expect appreciable nonlinear optical phenomena in thin atomic layered GaSe. Indeed, observations of second-harmonic generation (SHG) in few-layered GaSe sheets were reported early this year, where the emission photon energy exceeded the material bandgap with the signal significantly enhanced by resonating with optical dipole transitions.<sup>23</sup> However, at the monolayer limit and under nonresonant condition, it is still elusive whether SHG signal remains appreciable or not. Herein, for the first time we observed strong SHG signal in monolayer GaSe under the nonresonant condition that both the excitation and emission photon energies were within its optical bandgap. The nonresonant SHG intensity of GaSe is the strongest among all the 2D atomic crystals measured up to day. For instance, at the excitation wavelength of 1600 nm, the SHG signal from monolayer GaSe is 1-2 orders of magnitude larger than that from monolayer MoS<sub>2</sub> under the same excitation power. The strong nonlinear signal enables us to use polarization-dependent SHG intensity and SHG mapping to investigate the structural symmetry information on this material. The monolayer GaSe shows 3-fold lattice symmetry that has a one-to-one correspondence to its geometric triangular shape. The bilayer GaSe exhibits two dominant stacking orders: AA and AB stacking, and their correlation to the interlayer twist angles indicates that the bottom and top layers have the same primary edge configuration.

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In monolayer GaSe, two layers of Ga atoms are sandwiched between two layers of Se atoms in an eclipsed fashion (Figure 1a).<sup>24,25</sup> The in-plane geometry of monolayer GaSe is a



**Figure 1.** Strong SHG in monolayer GaSe. (a) Schematic atomic structure of monolayer GaSe, two layers of Ga atoms sandwiched by two layers of Se atoms, consisting of vertically stacked Se–Ga–Ga–Se sheets. (b) In-plane configuration of monolayer GaSe is of hexagon structure with Ga atoms and Se atoms separately occupying the two sublattices. (c) AFM image of GaSe monolayer with about 0.83 nm thickness on mica substrate. The monolayer has triangular shape with lateral side length of ~15  $\mu$ m. (d) The nonlinear spectrum of monolayer GaSe under excitation of  $\lambda_{ex}$  = 1350 nm on fused silica substrate. The peak at 675 and 450 nm corresponds to the SHG and THG signals, respectively.

honeycomb structure in which Ga and Se atoms respectively occupy the two sublattices (Figure 1b). In multilayer GaSe, the adjacent monolayers are coupled by van der Waals interactions. For the monolayer study, in principle one can follow the process of graphite exfoliation method to prepare the sample. However, possibly due to different interlayer coupling strength between GaSe and graphite, no successful mechanical exfoliation of monolayer GaSe has been reported so far.<sup>22,23</sup> On the other hand, single-crystal GaSe monolayers have been grown on various substrates by chemical vapor deposition (CVD) method<sup>14-18</sup> (see methods for our growth details in Supporting Information, SI). Figure 1c shows one representative atomic force microscopic (AFM) image of a GaSe monolayer grown on mica. Its height of about 0.83 nm is in consistent with previous reported value for monolayer (~0.80 nm).<sup>17</sup>The CVD monolayer flake has an equilateral triangular shape, with edge lengths of ~15  $\mu$ m large enough for nonlinear optical measurements.

Monolayer GaSe belongs to noncentrosymmetric  $D_{3k}^{1}$  space group and therefore should have nonzero SHG signal.<sup>26–32</sup> But it is unclear whether the signal is strong enough for detection without the excitation power exceeding the materials damage threshold. To investigate the SHG signal from monolayer GaSe, we use a femtosecond OPO laser with tunable wavelength (see setup details in SI). Theoretical calculations within the density functional framework reveal that monolayer GaSe has a bandgap of ~2.3 eV, corresponding to an excitation wavelength of ~540 nm<sup>18,19</sup> (our optical reflection spectrum shows no peak under wavelength longer than 550 nm; see SI for details). In order to investigate the SHG signal under nonresonant conditions for both excitation and emission photon, we purposely tune the laser wavelength longer than twice of monolayer bandgap wavelength. Figure 1d shows one typical nonlinear spectrum of monolayer GaSe under excitation of  $\lambda_{ex}$  = 1350 nm on fused silica substrate. The spectrum shows a prominent peak at 675 nm, which is exactly half of the excitation wavelength. Therefore, the observed peak can be unambiguously assigned as SHG signal. (The peak at 450 nm corresponds to a third-harmonic generation, or THG, signal). We measured SHG signal under the other two excitation

wavelengths of  $\lambda_{ex}$  = 1210 and 1600 nm. In all these three wavelengths, strong SHG signals were observed (Figure 2a



**Figure 2.** SHG in monolayer GaSe under different wavelengths and excitation power. (a) SHG intensity from monolayer GaSe (solid lines) and MoS<sub>2</sub> (dashed lines) under different excitation wavelengths. The intensity corresponding to  $\lambda_{ex} = 1350$  (1375) and 1600 nm is magnified by 3 and 30 times, respectively. The theoretical optical bandgap of monolayer GaSe is around 540 nm, and the laser with two-photon emission wavelength closer to it generates stronger SHG. (b) The excitation power dependence of SHG intensity. The diagram is a plot of the natural logarithm. The SHG intensity shows a power-law dependence on the excitation power with the coefficient fitted to 2.1, which is very close to the theoretical value of 2 from the electric dipole theory.

solid lines), which proves the presence of strong optical nonlinearities in monolayer GaSe in a wide spectral range. Also, the intensity of the SHG signal follows a simple relation with the wavelength of excitation laser: shorter wavelength produces larger intensity. This behavior should be attributed to the fact that the energy of shorter wavelength SHG photon is closer to the optical bandgap of monolayer GaSe or closer to emission resonant condition.

We further investigated the dependence of SHG intensity on the laser excitation power. The electric dipole theory predicts that under the first-order perturbation  $I_{SHG} = |\mathbf{E}(2\omega)|^2 \propto |\mathbf{E}(2\omega)|^2$  $P(\omega)|^2$ , where  $I_{SHG}$ ,  $E(2\omega)$  and  $P(\omega)$  are the SHG intensity, SHG electric field vector, and excitation power, respectively.<sup>3</sup> As a result, the SHG intensity should show a quadratic dependence on the excitation power. Indeed, in our experiment, we found the exponent is about 2.1 (Figure 2b), which is very close to the theoretical value of 2. This agreement suggests that under our experimental conditions, the simple electric dipole theory describes the SHG phenomenon in monolayer GaSe quite well. In the context of the electric dipole theory, we can quantitatively estimate the optical second-order susceptibility  $(\chi^{(2)} = \chi^{(2)}_{bbb})$  of monolayer GaSe on fused silica substrate,<sup>33</sup> which gives ~2.4 × 10<sup>-9</sup>, 1.7 × 10<sup>-9</sup>, and 0.7 ×  $10^{-9}$  m/V for  $\lambda_{ex}$  = 1210, 1350, and 1600 nm, respectively (see details in SI). In comparison, the GaSe bulk has a  $\chi^{(2)}$  of around  $1.4 \times 10^{-10}$  m/V.<sup>22</sup> To evaluate the SHG effect of monolayer GaSe qualitatively in the 2D material family, we compared it with monolayer MoS<sub>2</sub>, which has the same symmetry and was widely investigated before. We measured the SHG signal of monolayer MoS<sub>2</sub> under nonresonant condition ( $\lambda_{ex}$  = 1600 nm), and the intensity is 1-2 orders of magnitude smaller than monolayer GaSe (Figure 2a, purple dashed line). As a matter of fact, under a nonresonant condition and of the same excitation power, the SHG intensity of monolayer GaSe is larger than that of any other 2D monolayer reported so far, including  $MoS_2$ ,  $WS_2$ ,  $WSe_2$ , and  $BN.^{26-29}$  The larger SHG intensity in GaSe monolayer mainly comes from its smaller  $n_{2\omega}$  and  $n_{\omega}$  and also larger  $\chi^{(2)}$  and d (see details in SI).

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The strong SHG from monolayer GaSe enables us to facilitate this signal to investigate the structural symmetry properties of this material. We first probed the crystalline lattice symmetry in monolayer by polarization-dependent SHG intensity. We detected the SHG intensity with emission field polarization parallel to excitation field. Monolayer GaSe has  $D^{1}_{3h}$  3-fold symmetry, and therefore for the parallel polarization component, its SHG intensity will exhibit a 6-fold rotational symmetry with SHG intensity varying with azimuthal angle  $\theta$  (as indicated in Figure 3a).<sup>26–30</sup> As shown in Figure 3b, the



**Figure 3.** The crystalline symmetry in monolayer GaSe as probed by polarization-dependent SHG intensity. (a) Optical image of a triangular GaSe monolayer on Si/SiO<sub>2</sub> substrate. Azimuthal angle  $\theta$  is defined as the polarization direction (for both excitation and emission) relative to one triangular lateral side direction. (b) The polarization angle  $\theta$  dependent SHG intensity. It exhibits a clear sixfold rotational symmetry ( $I = I_0 \sin^2(3\theta)$ ). (c) The crystalline lattice model of monolayer GaSe, derived from the polarization-dependent pattern in (b). It has a one-to-one correspondence to the geometric triangular shape in (a).

polarization-resolved SHG intensity shows a clear six-petal pattern, which directly reveals the underlying symmetry and orientation of GaSe monolayer. This angle dependence can be described as  $I = I_0 \sin^2(3\theta)$ , where I and  $I_0$  are the SHG intensity and the maximum intensity of SHG response, respectively. From the symmetry analysis of  $D_{3h}^{1}$  monolayers,<sup>26-30</sup> the maximum petal direction is parallel to the inplane Ga-Se or Se-Ga direction. However, though the electrical dipole directions of Ga-Se and Se-Ga bonds are opposite in plane, since the SHG intensity is not phase sensitive, we cannot distinguish between the Ga-Se and Se-Ga bond alignments from the polarization-dependent signal, i.e., we do not know whether the Ga-Se bond direction is parallel or antiparallel to the petal direction yet. Therefore, the equilateral triangular clusters may correspond to clusters with a Se or Ga terminated zigzag edge. We show one possible structural model in Figure 3c.

We further employed the SHG mappings to investigate the stacking orders in GaSe bilayers. In general, the GaSe bilayers can exhibit two stable stacking configurations derived from the bulk crystal structures ( $\varepsilon$ - and  $\beta$ -phase).<sup>22</sup> We name the two configurations as AA and AB stacking, following the conventions in bilayer MoS2.31 In the AA stacking case, the in-plane Ga-Se bond direction is the same for the two layers, while in the AB-stacking case, the in-plane Ga-Se bond direction is opposite. AA-stacked bilayer still belongs to noncentrosymmetric  $D_{3h}^1$  group as in monolayer and, therefore, should have a strong SHG signal. The electric dipole theory predicts that the SHG signal in AA-stacked bilayer will be four times that of the monolayer (the SHG electric fields of the two layers are in phase). In contrast, AB-stacked bilayer belongs to the centrosymmetric  $D_{3d}^1$  group and, therefore, has no appreciable SHG signal (the SHG electric fields of the two layers are out of phase). In our CVD samples, the bilayers

predominantly have two configurations with twist angle of  $\phi = 0^{\circ}$  (Figure 4a) and  $\phi = 60^{\circ}$  (Figure 4d), where  $\phi$  is defined as



**Figure 4.** The stacking order in GaSe bilayers as probed by SHG imaging. (a–c) Optical image, SHG mapping, and atomic lattice model for GaSe bilayer with twist angle of  $\phi = 0^{\circ}$ . (d–f) Optical image, SHG mapping, and atomic lattice model for GaSe bilayer with twist angle of  $\phi = 60^{\circ}$ . These results reveal that the Ga–Se bond direction is the same (opposite) in the parallel (antiparallel) triangular monolayers.

the angle between the angular bisector of each triangle. In our SHG mapping, we observed that  $\phi = 0^{\circ}$  bilayer gives rise to enhanced SHG signal (Figure 4b), while the  $\phi = 60^{\circ}$  bilayer gives nearly zero SHG signal (Figure 4e). This result reveals that the  $\phi = 0^{\circ}$  bilayer belongs to the AA stacking (Figure 4c), while  $\phi = 60^{\circ}$  bilayer belongs to the AB stacking (Figure 4f). Therefore, the Ga–Se bond directions in the parallel GaSe triangles are parallel to each other, instead of antiparallel.

The two facts that the monolayer GaSe triangle has a one-toone correspondence to the lattice symmetry and the Ga–Se bond direction in the two parallel layers of GaSe bilayers is the same indicate that different triangular GaSe atomic layers may have the same dominant edge configurations. A direct experimental identification of the edge type of our CVDgrown sample can be obtained in the future by scanning tunneling microscope with a special conducting substrate that is compatible with GaSe CVD growth or by high-resolution transmission electron microscope<sup>34</sup> (but the electron beam irradiation may cause the reconstruction of the edge configuration<sup>35</sup>).

In summary, we report the first observation of strong SHG in monolayer GaSe under nonresonant excitation and emission condition. The nonresonant SHG intensity of GaSe monolayer is the strongest among all the 2D atomic crystals measured up to day. Further polarization-dependent SHG intensity and SHG mapping reveal that the monolayer GaSe shows 3-fold lattice symmetry with an intrinsic correspondence to its geometric triangular shape in our growth condition; whereas the bilayer GaSe exhibits two dominant stacking orders: AA and AB stacking. Our observations also indicate that the dominant edge configuration in different GaSe triangles is the same. Our work demonstrates that the SHG spectroscopy can be potentially applied to study the in-plane grain boundary in monolayer GaSe or the stacking orders in few-layered GaSe. The strong nonlinear optical responses in mono- and few-layered GaSe also provide a platform to explore nonresonance properties of 2D materials.

# ASSOCIATED CONTENT

### **S** Supporting Information

Growth of GaSe monolayer and bilayers, SHG measurements, reflection spectrum measurements, and second-order nonlinear susceptibility calculation. The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/jacs.5b04305.

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### Notes

The authors declare no competing financial interest.

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